



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/22

Paper 22

March 2020

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the March 2020 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **11** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

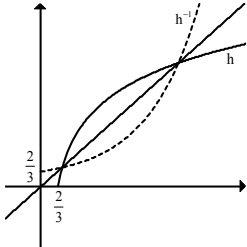
Question	Answer	Marks	Partial Marks
1	Expands right hand side and attempts to collect terms	M1	
	Factorises or solves <i>their</i> 3-term quadratic	M1	
	correct CVs $\frac{2}{5}$, $\frac{3}{2}$	A1	
	$\frac{2}{5} < x < \frac{3}{2}$ mark final answer	A1	FT <i>their</i> CVs, provided both M marks awarded

Question	Answer	Marks	Partial Marks
2	Valid method to find m $m = \frac{9-7}{10-6} \left[= \frac{1}{2} \right]$	M1	
	Valid method to find c e.g. $7 = \text{their} \frac{1}{2} \times 6 + c$	M1	FT <i>their m</i>
	$\lg y = \left(\text{their} \frac{1}{2} \right) x^3 + \text{their} 4$	M1	
	$y = 10^{\frac{1}{2}x^3+4}$ oe, isw	A1	
3	Rewrites in quadratic form soi e.g. $y = 3^x$ then $y^2 - 3y - 4 = 0$ or $(3^x)^2 - 3(3^x) - 4 = 0$	M1	
	Factorises or solves <i>their</i> 3-term quadratic e.g. $(y+1)(y-4) [= 0]$ or $(3^x+1)(3^x-4) [= 0]$	M1	
	$3^x = 4$	A1	ignore $3^x = -1$
	$x = \log_3 4$ or $\frac{\ln 4}{\ln 3}$ oe, only	A1	
4	$\overline{OC} - \overline{OA} = 4(\overline{OC} - \overline{OB})$ soi	B1	
	$[\overline{OC} =] \begin{pmatrix} 15 \\ -3 \end{pmatrix}$	B2	B1 for $[x =] 15$ or $[y =] -3$
	$ \overline{OC} = \sqrt{\text{their} 15^2 + \text{their} (-3)^2}$	M1	
	$\frac{1}{\sqrt{234}} \begin{pmatrix} 15 \\ -3 \end{pmatrix}$ oe	A1	FT <i>their</i> $\begin{pmatrix} 15 \\ -3 \end{pmatrix}$ and <i>their</i> $\sqrt{234}$
5(a)	Correct V shape with vertex on positive x -axis	B1	
	$(0, 7)$	B1	
	$\left(\frac{7}{5}, 0 \right)$	B1	

Question	Answer	Marks	Partial Marks
5(b)	$x = 2$	B1	
	$5x - 7 = \text{their}(-3)$ oe, soi or $25x - 35 = \text{their}(-15)$ oe, soi	M1	
	$x = \frac{4}{5}$ oe	A1	
	Alternative method		
	$25x^2 - 70x + 40 = 0$ oe	(B1	
	factorising e.g. $(5x - 4)(x - 2)$	M1	
	$x = 2, \frac{4}{5}$	A1)	
6(a)	$2(6) + 6\theta = 2(6 + 5\pi)$ oe	M1	
	$\theta = \frac{5}{3}\pi$ oe, soi	A1	
	$\frac{1}{2} \times 6^2 \times \text{their}\left(\frac{5\pi}{3}\right)$	M1	
	94.2 or 30π	A1	
	Alternative method		
	arc $AB = 10\pi$	(M1	
	sector is $\frac{10\pi}{12\pi} = \frac{5}{6}$ of the circle	B1	
	$\frac{5}{6} \times 36\pi$	M1	
	94.2 or 30π	A1)	
6(b)	$2\left(7 \sin \frac{\pi}{8}\right) + \frac{7\pi}{4}$ oe, soi	M2	M1 for $2\left(7 \sin \frac{\pi}{8}\right) + \text{their}\left(\frac{7\pi}{4}\right)$ or $\text{their}\left(2\left(7 \sin \frac{\pi}{8}\right)\right) + \frac{7\pi}{4}$
	10.9 or 10.85 to 10.86	A1	

Question	Answer	Marks	Partial Marks
7	Eliminates one variable e.g. $x^2 = 5(x^2 - 2x + 1) - 1$ or $y = 5y - 1 - 2\sqrt{5y - 1} + 1$	M1	
	Collects terms ready to solve e.g. $4x^2 - 10x + 4 = 0$ or $4y^2 - 5y + 1 = 0$	A1	
	Factorises, applies the formula or completes the square e.g. $2(2x - 1)(x - 2)$ or $(4y - 1)(y - 1)$	M1	
	Both (0.5, 0.25) and (2, 1)	A2	A1 for either (0.5, 0.25) or (2, 1) provided nfww or $x = 0.5, 2$ or $y = 0.25, 1$
8(a)	Valid explanation e.g. Each value of x is mapped to a unique value of y .	B1	
8(b)	$-5 \leq f \leq 1$	B1	
8(c)	$a = 3, b = 0.75$ oe, $c = -2$	B4	B1 for $a = 3$ B1 for $c = -2$ M1 for $\frac{2\pi}{b} = \frac{8\pi}{3}$ oe A1 for $b = 0.75$ oe

Question	Answer	Marks	Partial Marks
9	$\frac{d(e^{3x})}{dx} = 3e^{3x}$ soi	B1	
	Applies product rule to e.g. numerator: <i>their</i> $(3e^{3x})\sin x + e^{3x}\cos x$	M1	or to $x^{-2}\sin x : x^{-2}\cos x + (-2x^{-3})\sin x$ or to $e^{3x} \times x^{-2} :$ $e^{3x} \times (-2x^{-3}) + \textit{their}(3e^{3x}) \times x^{-2}$
	Correct quotient rule: $\frac{x^2(\textit{their}(3e^{3x}\sin x + e^{3x}\cos x)) - 2x(e^{3x}\sin x)}{x^4}$	M1	or applies product rule for a second time e.g. : $x^{-2}(\textit{their}(3e^{3x})\sin x + e^{3x}\cos x) + (-2x^{-3})(e^{3x}\sin x)$
	Fully correct derivative; isw	A1	
	$\delta y = \textit{their}\left(\frac{dy}{dx}\Big _{x=0.5}\right) \times h$	M1	
	7.14h or 7.137[66...]h with coefficient rot to 4 or more figs isw	A1	Answer only, without working, scores SC1
10(a)(i)	Correct method to find inverse	M1	
	$g^{-1}(x) = \frac{1}{x-3}$ oe	A1	
10(a)(ii)	$g^{-1} \geq 1$ or $[1, \infty)$	B1	
10(a)(iii)	$3 < x \leq 4$ or $(3, 4]$	B2	B1 for 3 and 4 in an incorrect inequality or for $x > 3$ or $x \leq 4$

Question	Answer	Marks	Partial Marks
10(b)	Correct graph for h	B1	
	h^{-1} the reflection of h in $y = x$	B1	FT <i>their</i> h
	Both graphs drawn over the correct domain	B1	FT <i>their</i> h and h^{-1}
		B1	Correct graphs intersecting twice
11	$h = \frac{1000}{\pi r^2}$ or $r = \sqrt{\frac{1000}{\pi h}}$ soi	B1	
	$S = \pi r^2 + 2\pi r \left(\frac{1000}{\pi r^2} \right)$ oe or $S = \pi \left(\frac{1000}{\pi h} \right) + 2\pi \sqrt{\frac{1000}{\pi h}} (h)$ oe	M1	
	$S = \pi r^2 + 2 \left(\frac{1000}{r} \right)$ or better or $S = \frac{1000}{h} + 2\pi \sqrt{\frac{1000}{\pi}} \left(h^{\frac{1}{2}} \right)$	A1	
	$\frac{dS}{dr} = 2\pi r - 2000r^{-2}$ or $\frac{dS}{dh} = -1000h^{-2} + \sqrt{1000\pi} h^{-\frac{1}{2}}$	B2	B1 FT for each term correct
	$\frac{dS}{dr} = 0, r^3 = \frac{1000}{\pi}$ oe or $\frac{dS}{dh} = 0, h^{\frac{3}{2}} = \sqrt{\frac{1000}{\pi}}$ oe	M1	
	$S = \pi \left(\sqrt[3]{\frac{1000}{\pi}} \right)^2 + \frac{2000}{\sqrt[3]{\frac{1000}{\pi}}}$ or $S = \frac{1000}{\sqrt[3]{\frac{1000}{\pi}}} + 2\sqrt{1000\pi} \left(\sqrt[3]{\frac{1000}{\pi}} \right)^{\frac{1}{2}}$	M1	
	439 or 439.3 to 439.4	A1	

Question	Answer	Marks	Partial Marks
12(a)	$v = -6t + c$ soi	B1	
	$v = -6t + 18$	M1	
	$-6t + 18 = 0, t = 3$	A1	
12(b)	$s = \frac{-6t^2}{2} + 18t$ soi	B1	
	$(-3(3)^2 + 18(3)) - (-3(2)^2 + 18(2))$	M1	FT <i>their s</i> provided it is from an attempt to integrate
	3 (metres)	A1	Not from wrong working
13(a)(i)	$a + ar = 10$ soi	B1	
	$ar^2 = 9$ soi	B1	
	Solves <i>their</i> equations	M1	
	$r = -\frac{3}{5}, \frac{3}{2}$ and $a = 25, 4$	A2	A1 for either $r = -\frac{3}{5}, \frac{3}{2}$ or $a = 25, 4$ or for $r = -\frac{3}{5}$ and $a = 25$ or for $r = \frac{3}{2}$ and $a = 4$
13(a)(ii)	$\frac{125}{8}$ or 15.625 or $15\frac{5}{8}$ only	B1	

Question	Answer	Marks	Partial Marks
13(b)	$d = 8$	B1	
	$[S_{200} - S_{99} =]$ $\frac{200}{2}\{2(-10) + 199(\text{their } 8)\} -$ $\frac{99}{2}\{2(-10) + 98(\text{their } 8)\}$ oe	M2	M1 for either sum correct or correct FT their d
	119382 cao	A1	
	Alternative method 1		
	$d = 8$	(B1	
	$u_{100} = -10 + 99 \times 8 [= 782]$ and $u_{200} = -10 + 199 \times 8 [= 1582]$ and $n = 101$	M1	
	$\frac{1}{2}(101)(782 + 1582)$	M1	
	119382 cao	A1)	
	Alternative method 2		
	$d = 8$	(B1	
	$u_{100} = -10 + 99 \times 8 [= 782]$ and $n = 101$	M1	
	$\frac{1}{2}(101)(2 \times 782 + (101 - 1) \times 8)$	M1	
	119382 cao	A1)	